Supplemental Material

Supporting Information for "Response of Vertical Velocities in Extratropical Precipitation Extremes to Climate Change"

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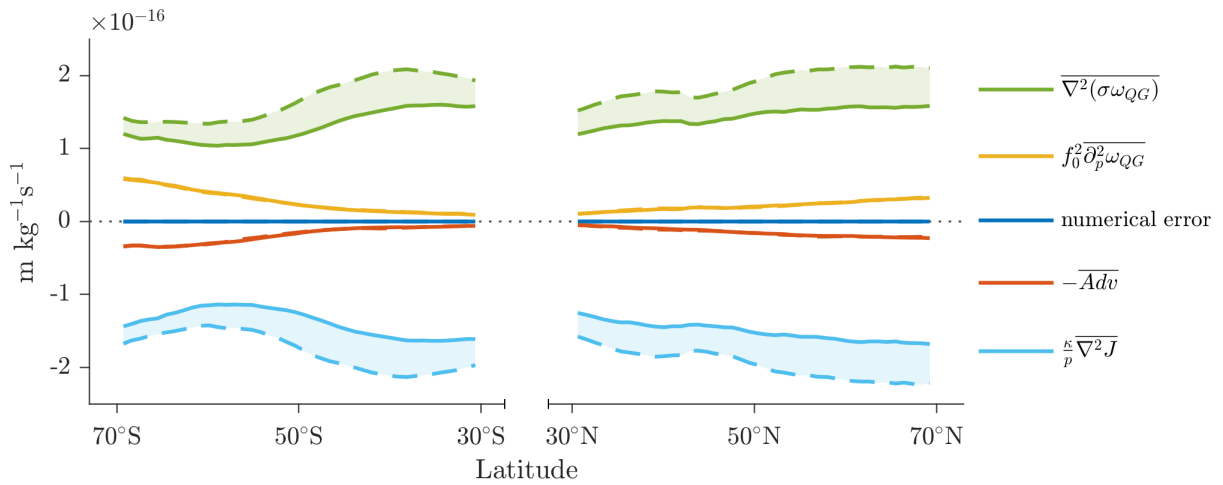**ziweili@mit.edu*

Figure S1. Event- and zonal-mean of terms in the QG-ω equation (Eq. 1) at 500hPa for extratropical precipitation extremes in CESM-LE. Solid lines indicate historical, dashed lines indicate RCP8.5, and shading indicates the response to climate change. Terms on the right-hand side of the equation are shown with a minus sign so that the sum is zero. The darker blue line gives the error in the numerical solution of the QG-ω equation.
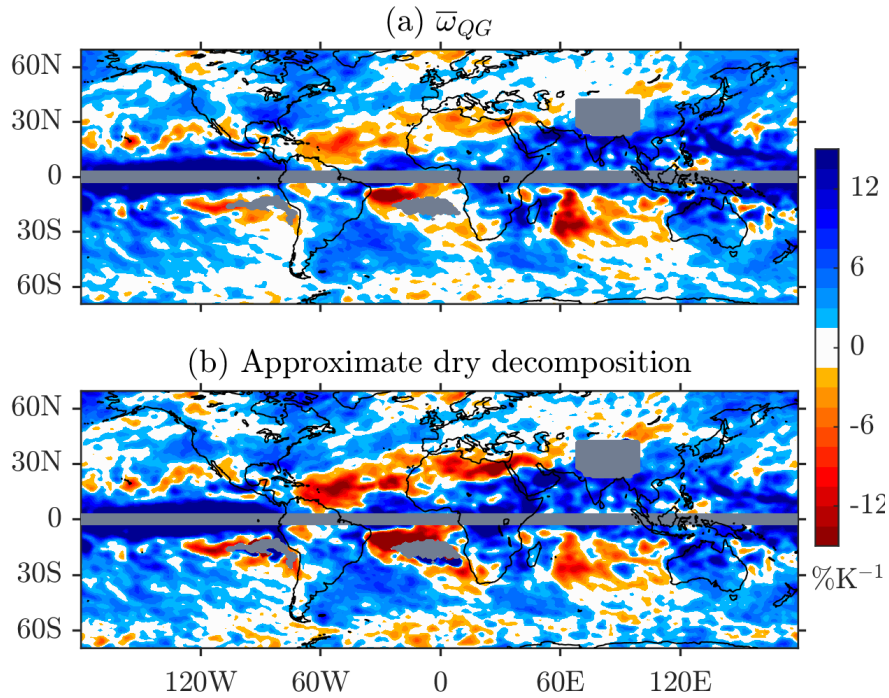
Figure S2. Changes in $\overline{\omega}_{\mathrm{QG}}$ (a) from the numerical inversions of the QG-ω equation and (b) as estimated from the approximate dry decomposition (Eq. 7) for vertical velocities at 500hPa associated with precipitation extremes in CESM-LE. Results are expressed as percentage changes relative to the historical climate and normalized by the increase in global-mean surface temperature. Masking and smoothing are as in Fig. 2.
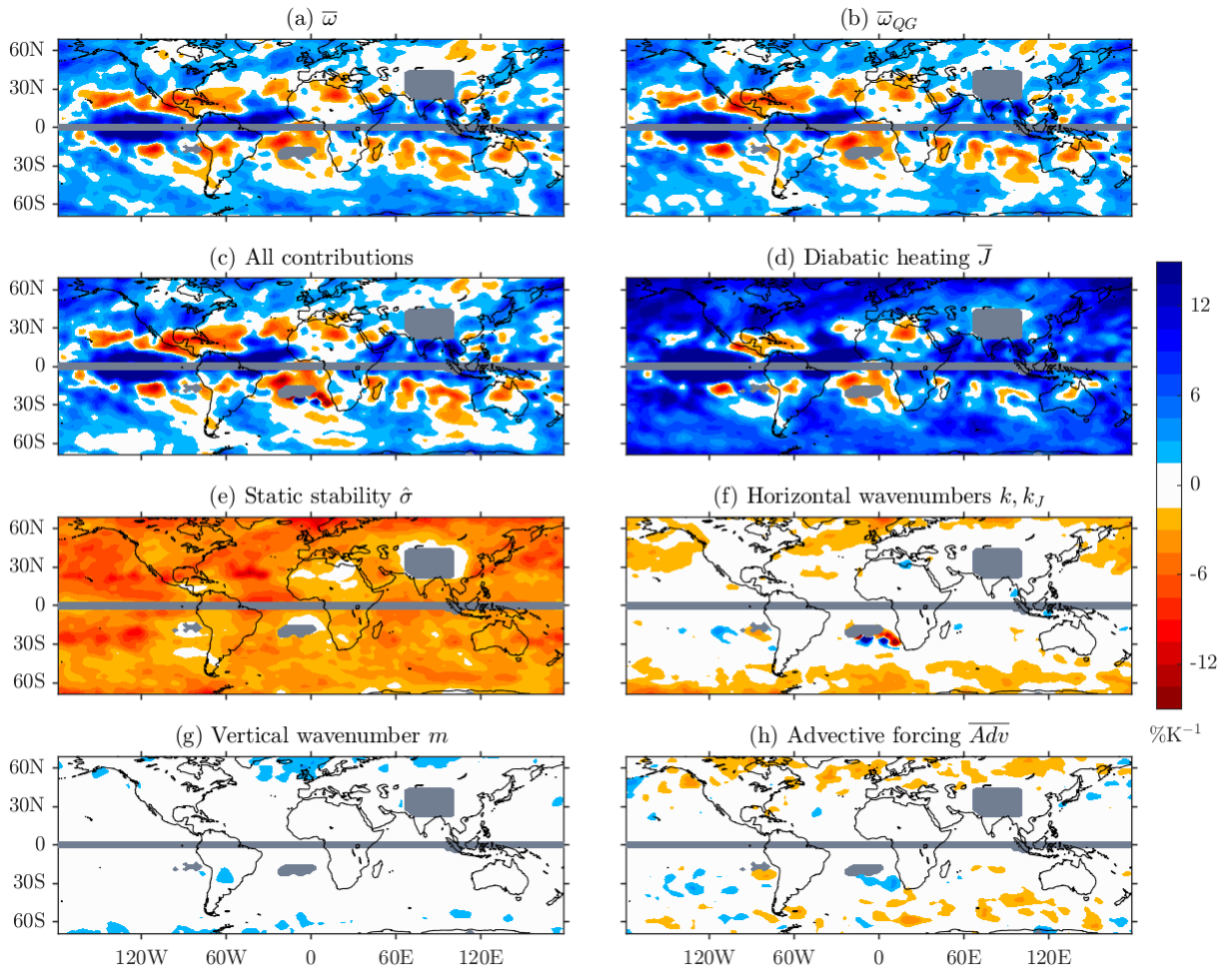
Figure S3. As in Fig. 4, but for 6-hourly events with GFDL-CM3. Grid points with fewer than 15 events are masked.
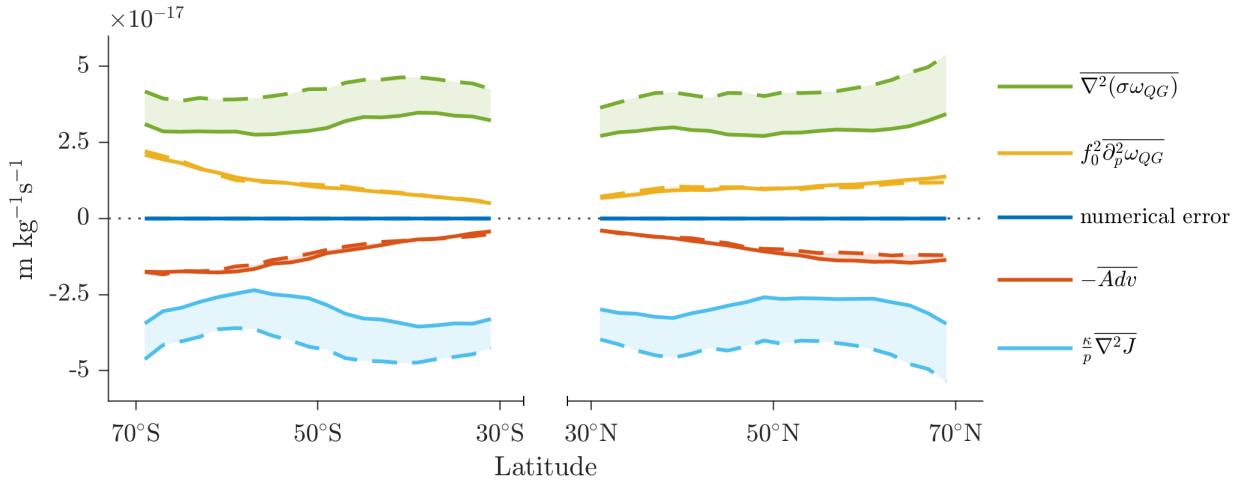

Figure S4. As in Fig. S1, but for GFDL-CM3. (Note the change of scale of the vertical axis)
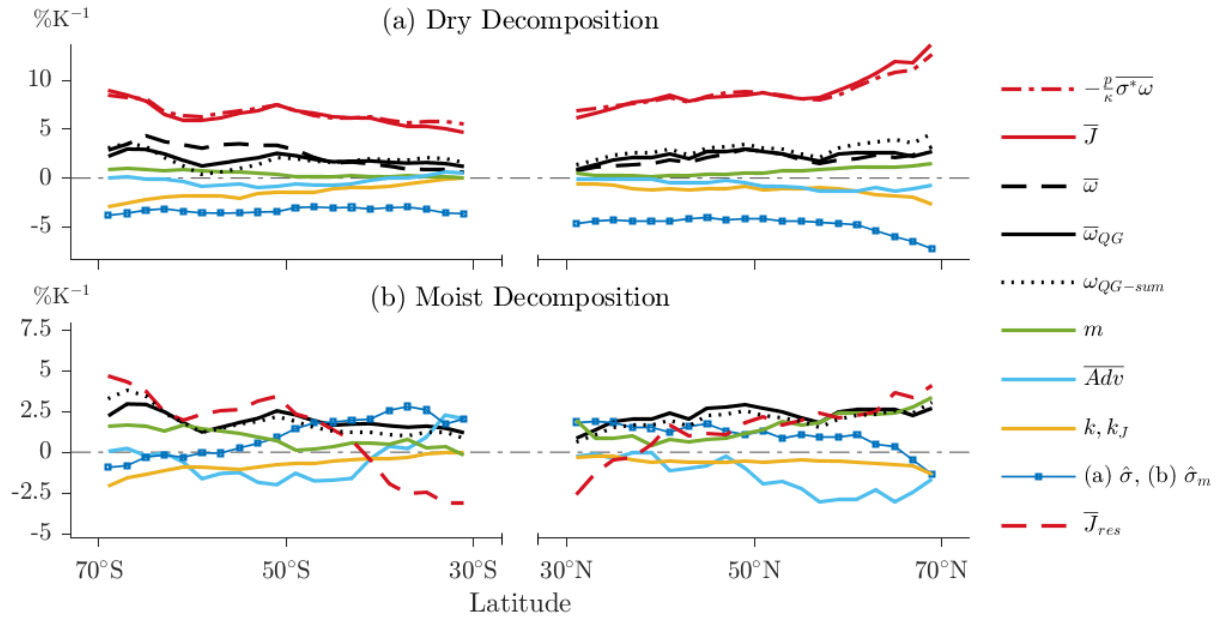
Figure S5. As in Fig. 5, but for GFDL-CM3. (Note the change of scale of the vertical axis)
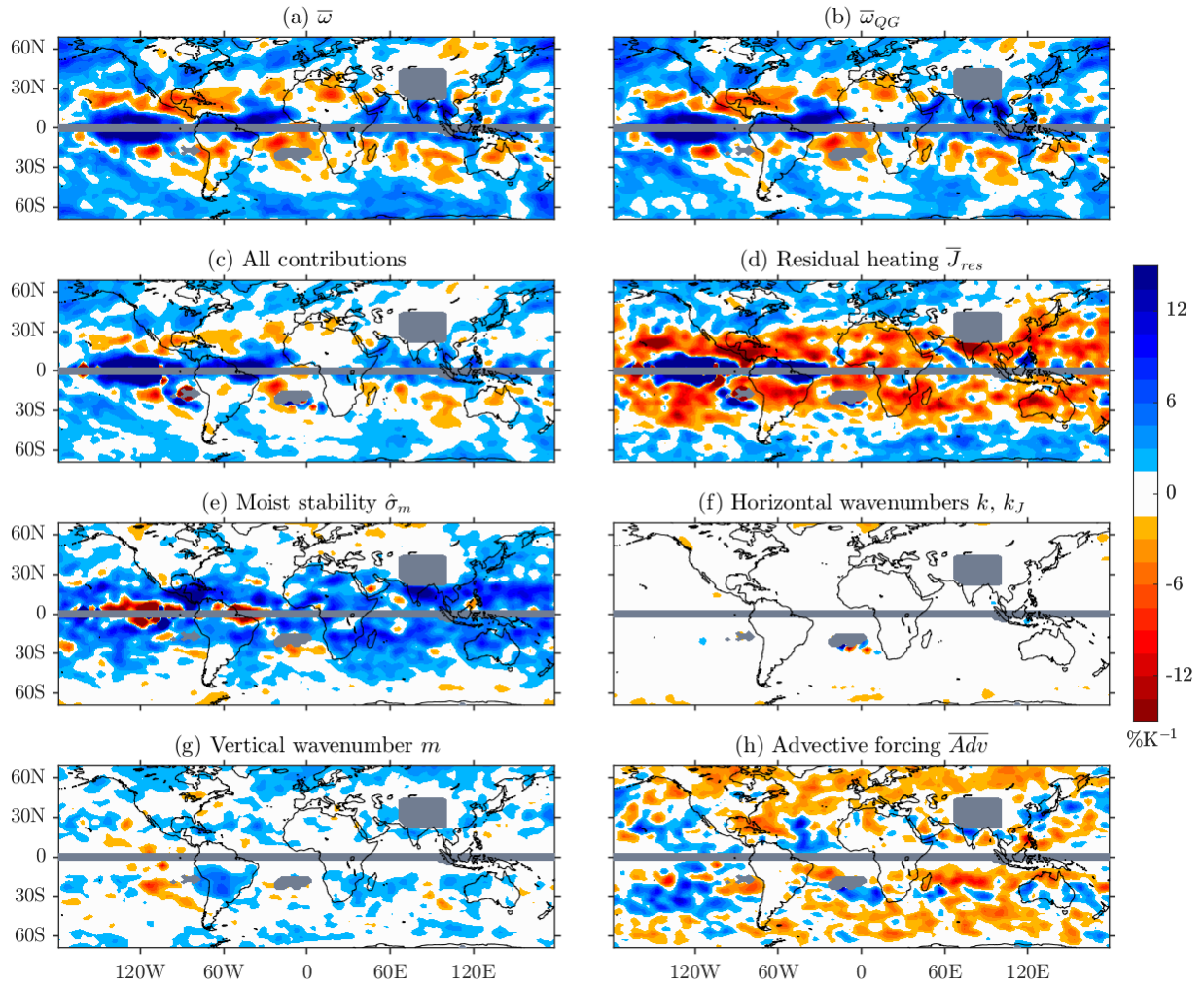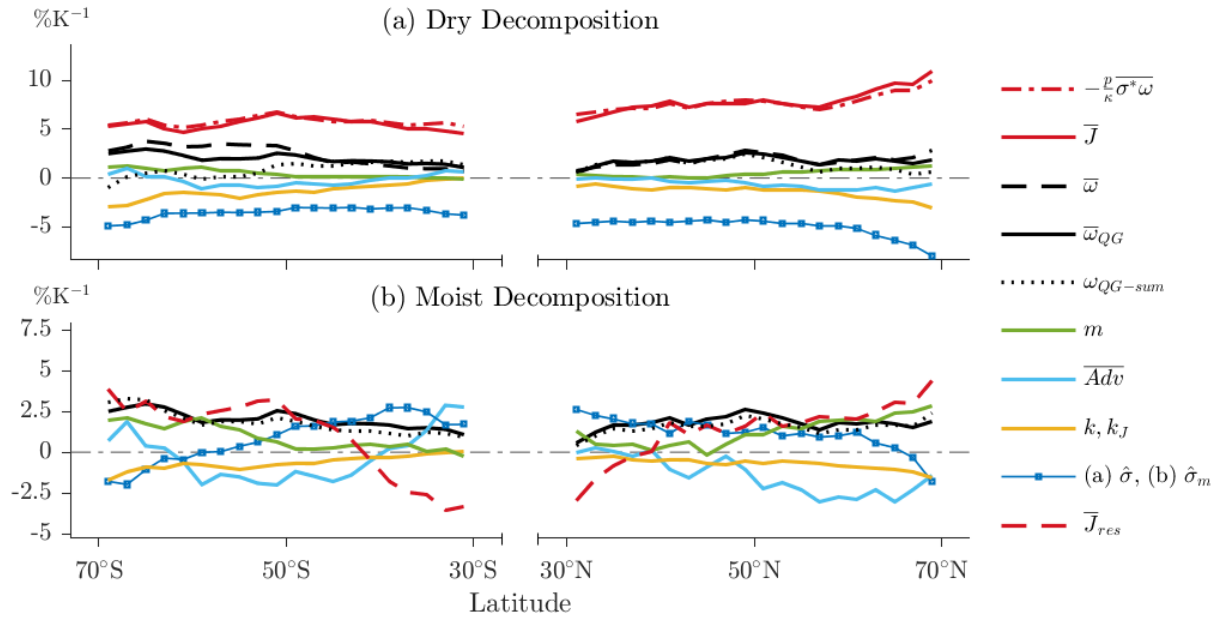
Figure S6. As in Fig. 8, but for GFDL-CM3.

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Figure S7. As in Fig. 5, but for GFDL-CM3 and the QG-ω equation is solved using ω taken from the GCM simulations for the lateral- and lower-boundary conditions.

Figure S8. As in Fig. 8, but for GFDL-CM3 and the QG-ω equation is solved using ω taken from the GCM simulations for the lateral- and lower-boundary conditions.
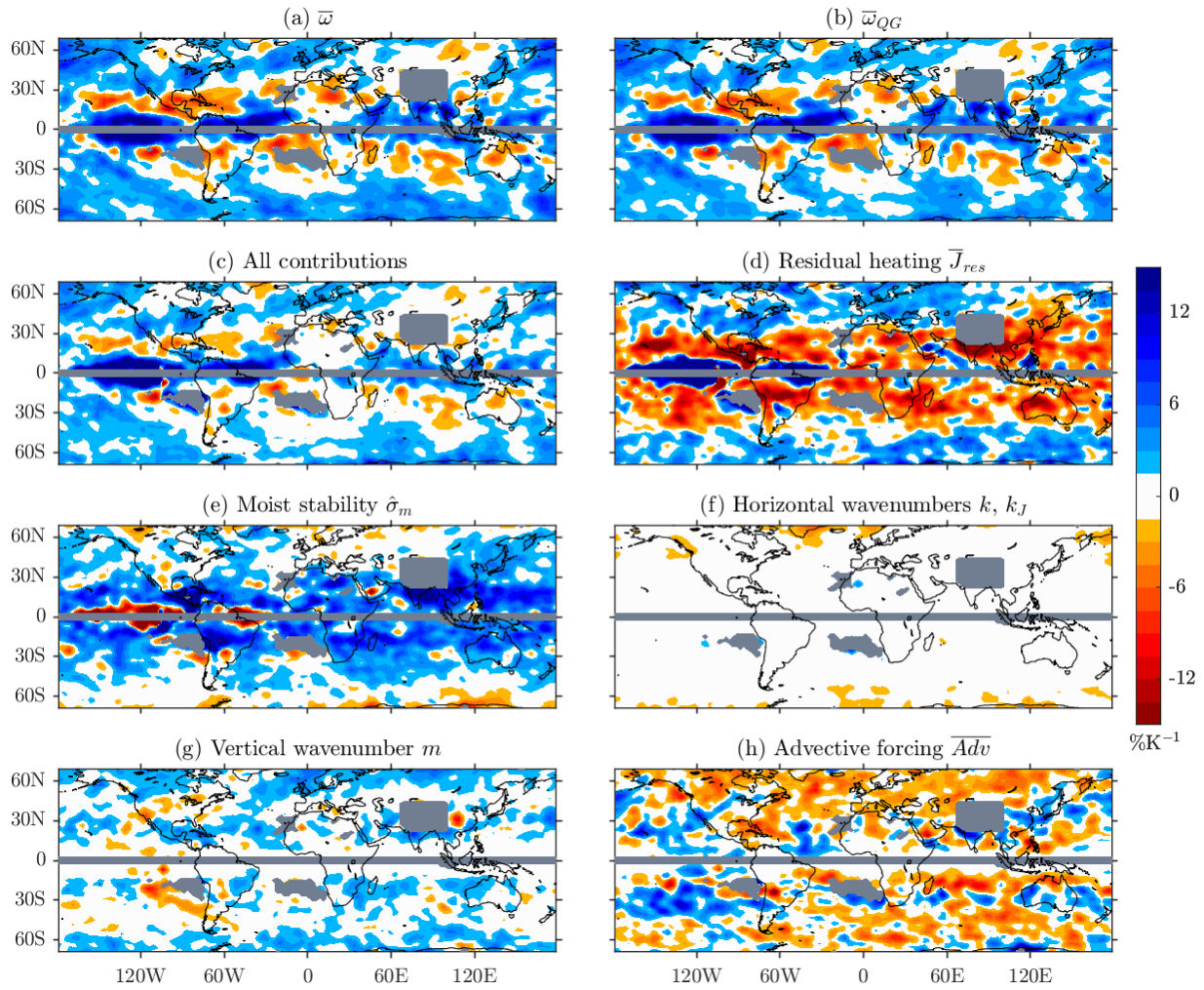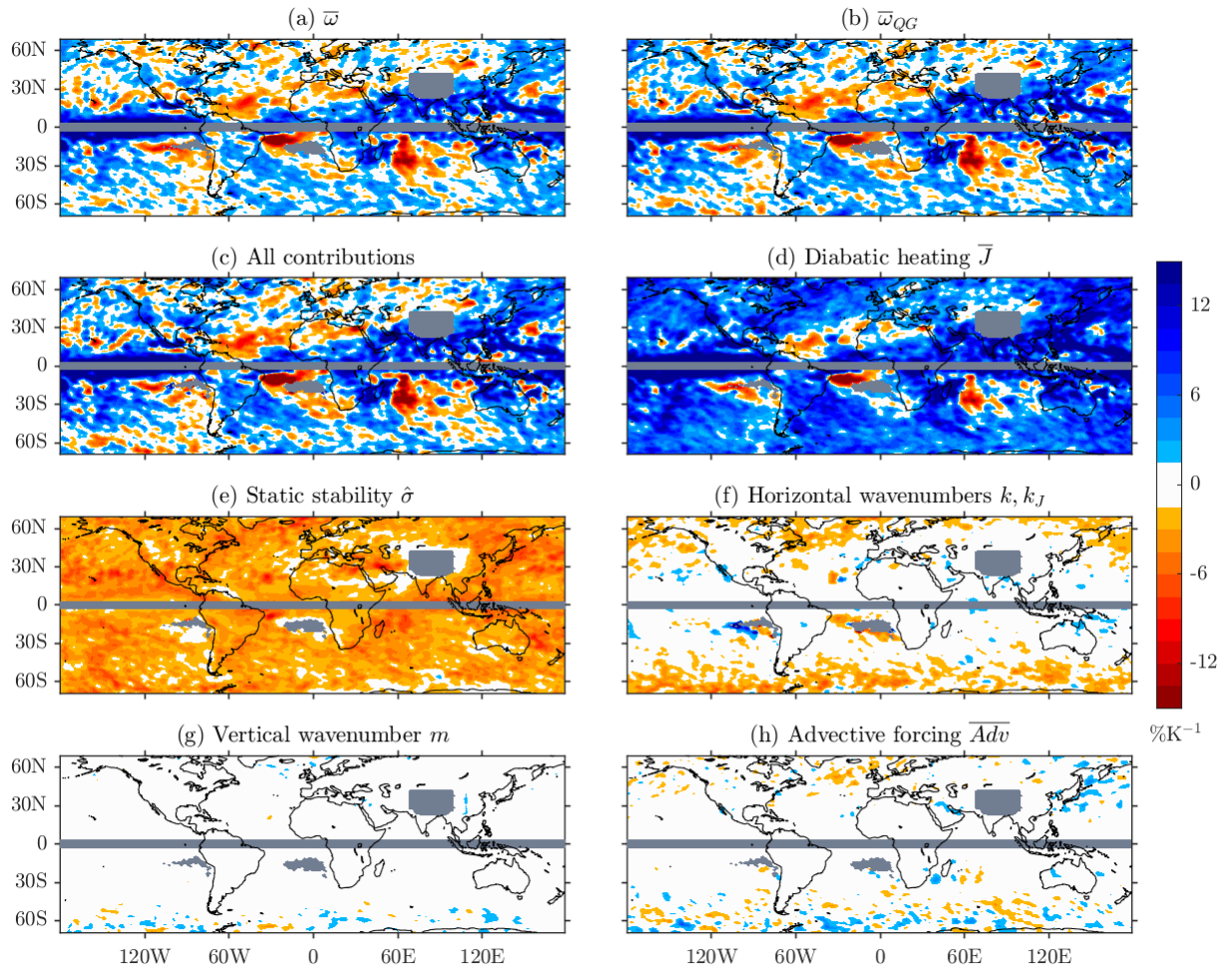
Figure S9. As in Fig. 4, but for daily precipitation extremes in CESM-LE, and grid points with fewer than 5 events are masked.
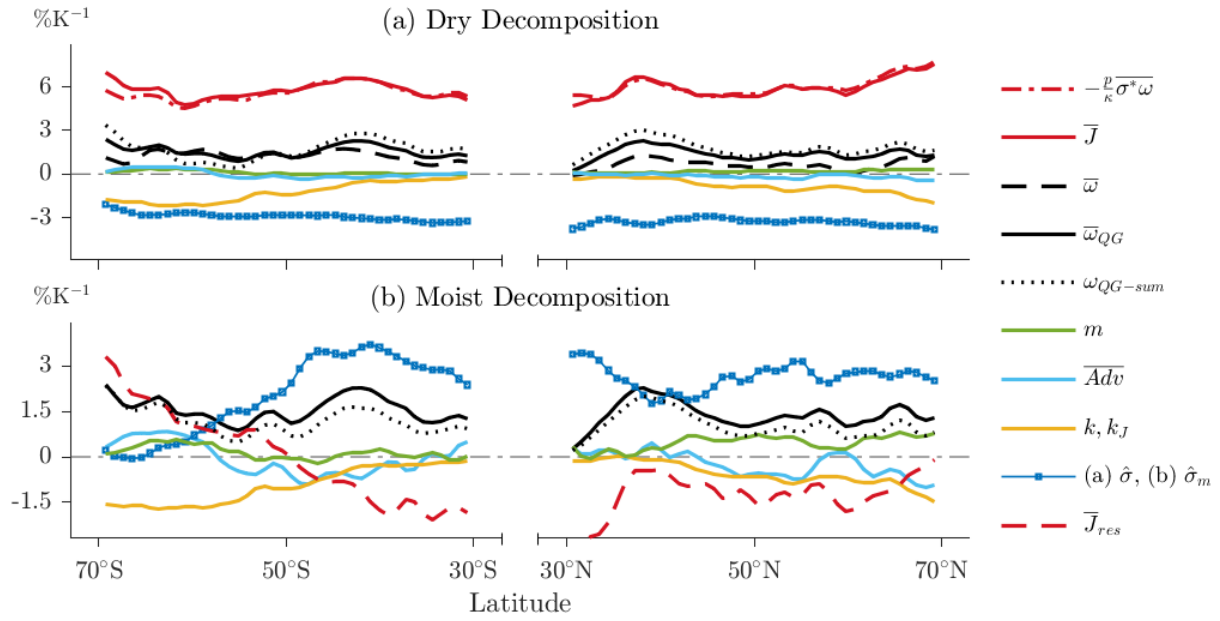
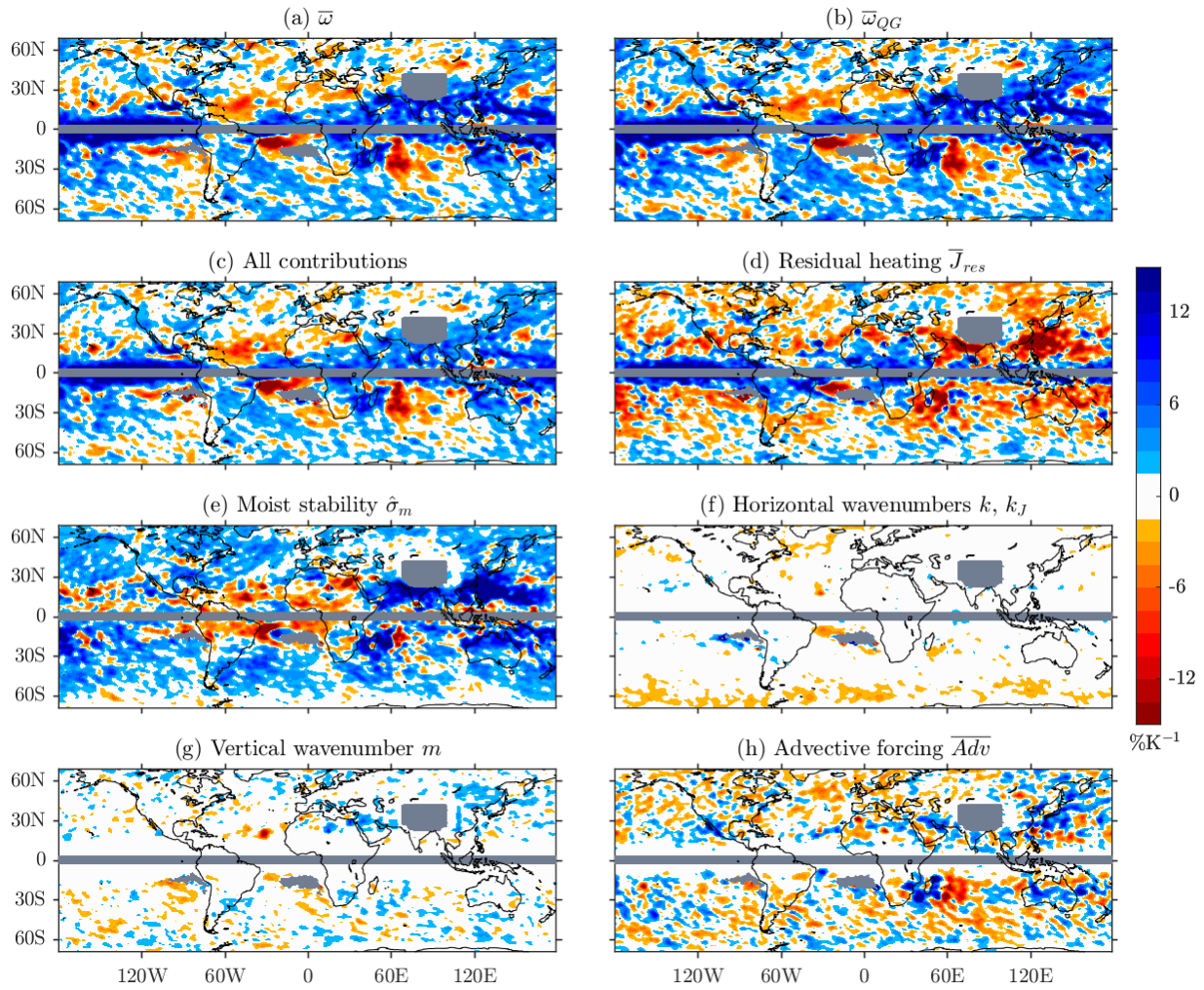**Figure S10.** As in Fig. 5, but for daily precipitation extremes in CESM-LE.

Figure S11. As in Fig. 8, but for daily precipitation extremes in CESM-LE, and grid points with fewer than 5 events are masked.
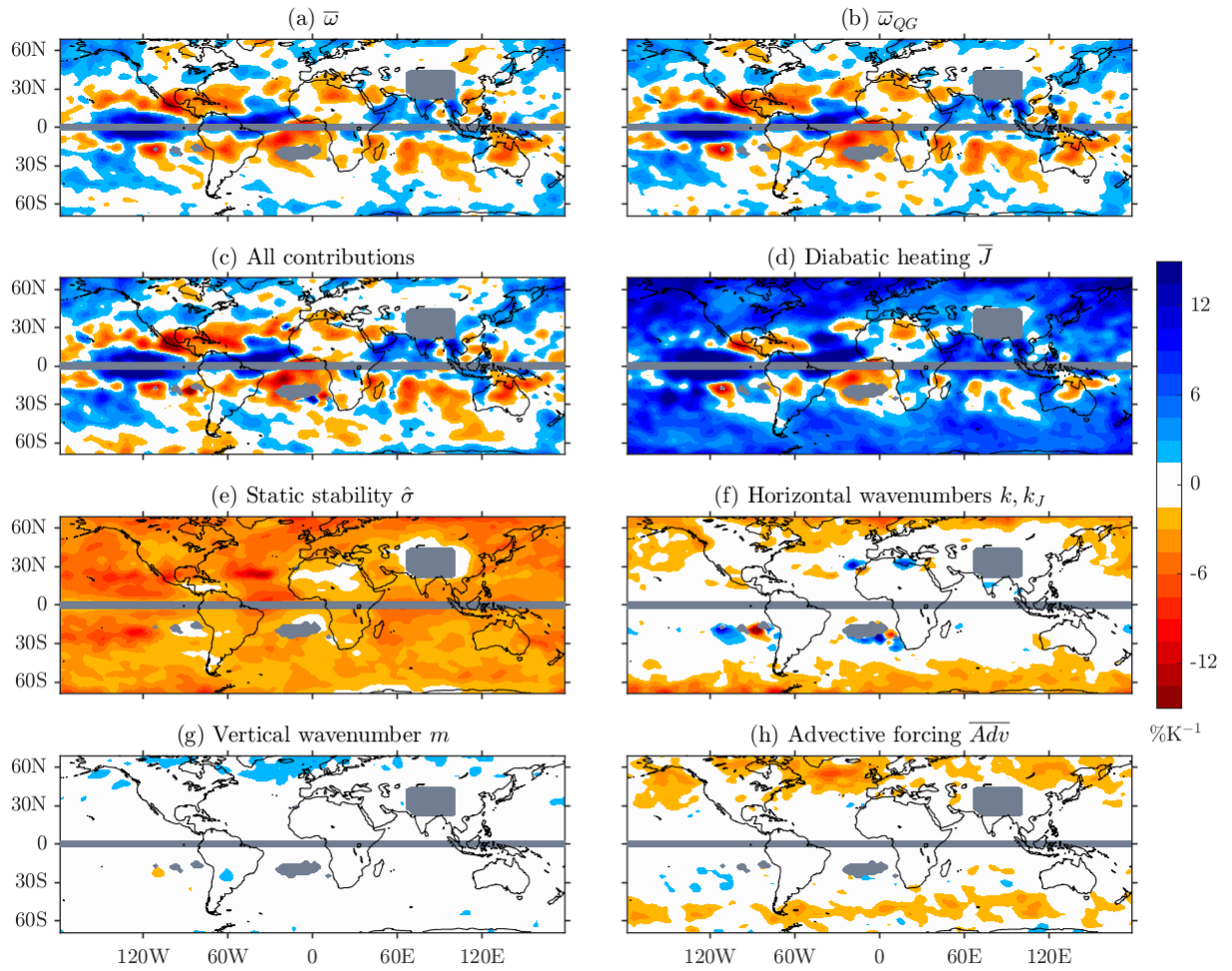
Figure S12. As in Fig. 4, but for daily precipitation extremes at the 99.5-percentile in GFDL-CM3, and grid points with fewer than 5 events are masked.
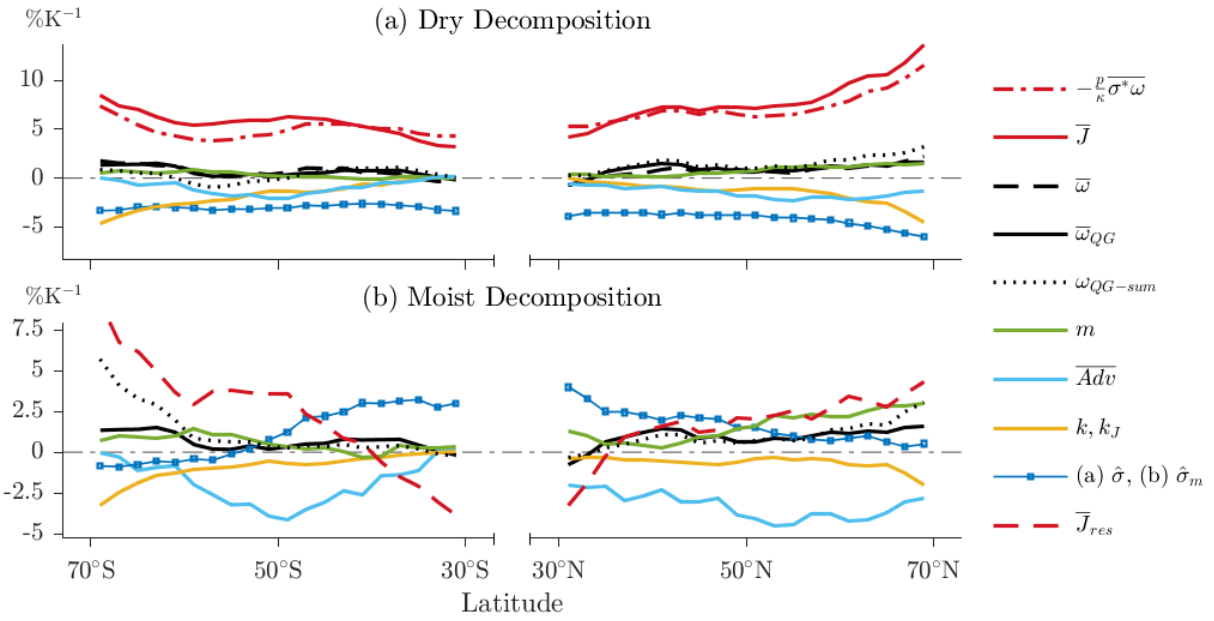
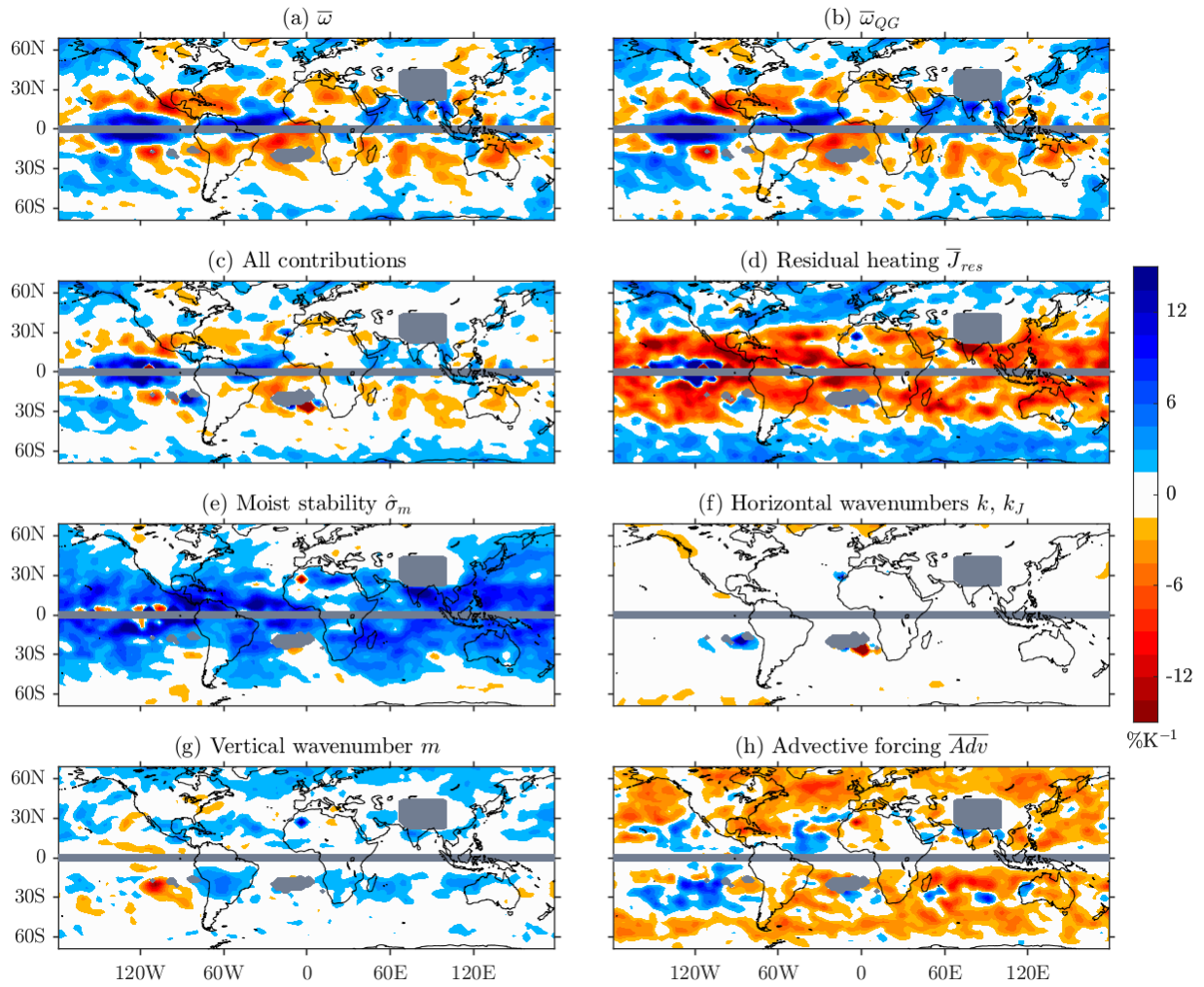**Figure S13.** As in Fig. 5, but for daily precipitation extremes at the 99.5-percentile in GFDL-CM3.

Figure S14. As in Fig. 8, but for daily precipitation extremes at the 99.5-percentile in GFDL-CM3.

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